

# Cochran's Q Test

**COCHRAN'S Q** test is used to verify if  $k$  treatments have the same effect between three or more related groups. In essence, the Cochran's Q test is an extension of the McNemar test [SDN]. While the results of Cochran's Q test are informative, one should also measure the degree of agreement among the tests.

## How To

- ✓ Run: **STATISTICS->NONPARAMETRIC STATISTICS -> COCHRAN'S Q TEST.**
- ✓ Select variables with a two-way randomized block design (rows are subjects, columns are treatments).
- ✓ **LISTWISE** deletion is used for missing values removal.

## Results

The report includes Cochran's Q test results and the table with proportions statistics for each variable.

Cochran's Q Test			
Sample size	12	Degrees of Freedom	3
Test Statistics Q	13.28571	p-level	0.00406
Statistics			
VAR	Sum	Proportions: 0	Proportions: 1
$\alpha$	4	66.66667%	33.33333%
$\beta$	3	75.0%	25.0%
$\gamma$	2	83.33333%	16.66667%
$\delta$	10	16.66667%	83.33333%

The Cochran's Q test statistic is defined as following:

$$T = k(k - 1) \frac{\sum_{j=1}^k (x_j - \frac{N}{k})^2}{\sum_{i=1}^b x_i (k - x_i)}$$

where  $k$  is the number of treatments,  $x_j$  is the column total for the  $j^{\text{th}}$  treatment,  $x_i$  is the row total for the  $i^{\text{th}}$  block,  $b$  is the number of blocks,  $N$  is the total number of observations. The null hypothesis is accepted if  $Q$  is less than critical  $\chi^2$ , and rejected if  $Q > \chi^2$ .

If **P-LEVEL** is less than  $\alpha$  (default value – 0.05) then the  $H_0$  (the treatments are equally effective) is rejected and it is concluded that the significant difference among treatments exists.

## **Assumptions**

The Cochran's Q test is based on the following assumptions:

- a) The sample of  $n$  subjects has been randomly selected from the population it represents;
- b) The scores of subjects are in the form of a dichotomous categorical variable (i.e., a "0" or "1").

## **References**

[SDN] Sheksin, David (2000) Handbook of Parametric and Nonparametric Statistical Procedures. SECOND EDITION Chapman & Hall/CRC